

# Stochastic, Spatially Explicit Models

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# Model Categorizations

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- Continuous vs. Discrete
- Compartmental (SI, SIS, SIR, SLICR...)  
vs. Individual Based (Microsimulation Model)
- Behavioral, Descriptive, and Normative
- Analytic vs. Numeric
- **Deterministic vs. Stochastic**
- **Spatial vs. Non-spatial**



# Deterministic vs. Stochastic

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- Deterministic
  - Single input/output
  - No element of chance
  - Mean, median, mode, 95<sup>th</sup> or 99<sup>th</sup>%, extreme value(s)
- Stochastic (probabilistic or random)
  - Incorporates an element of chance
  - Reflects uncertainty and variability
  - Multiple input values and outputs
  - Statistical distribution based

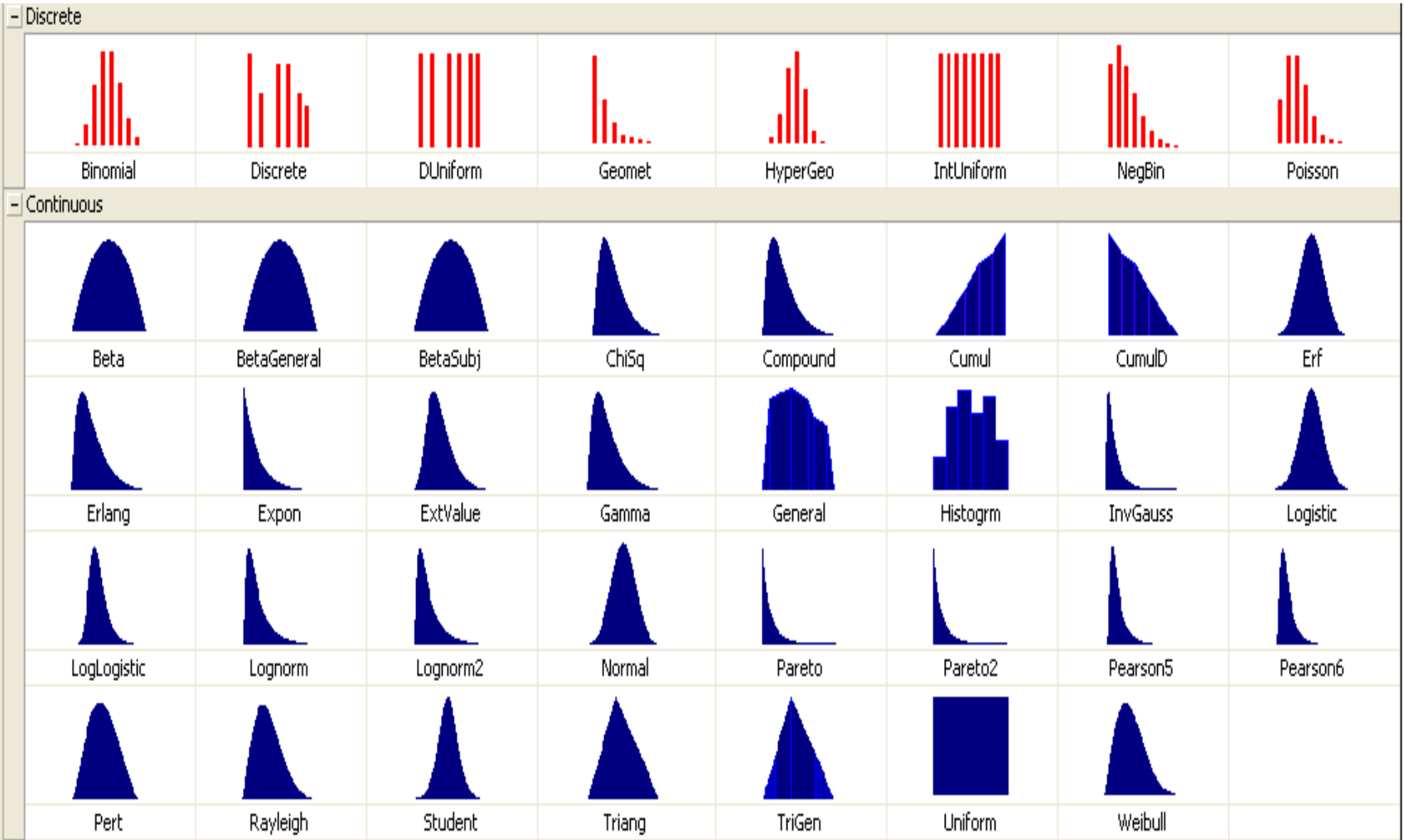


# Defining Stochastic Inputs

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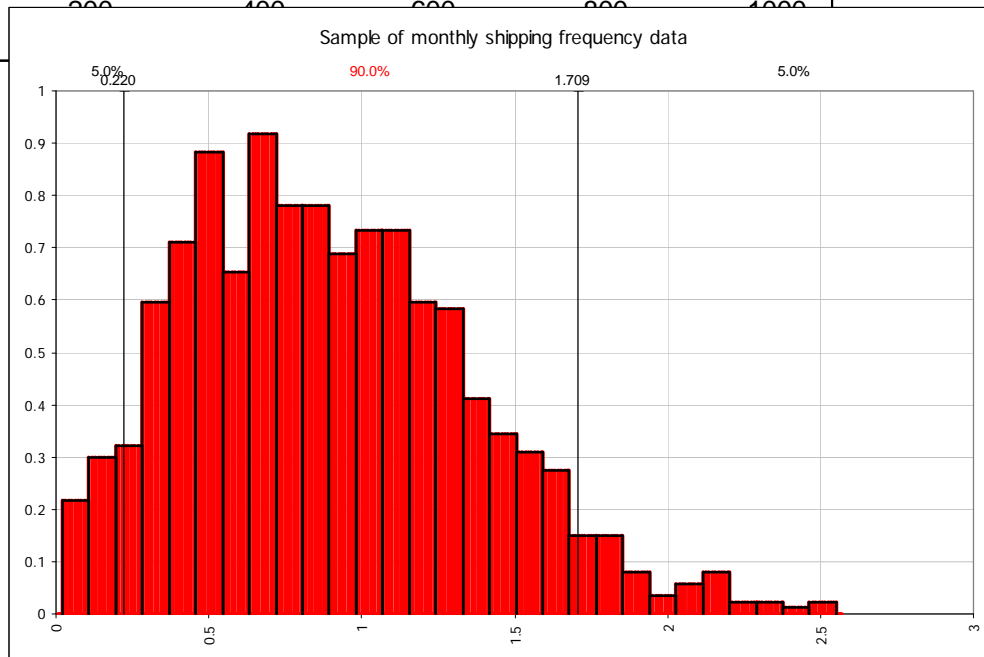
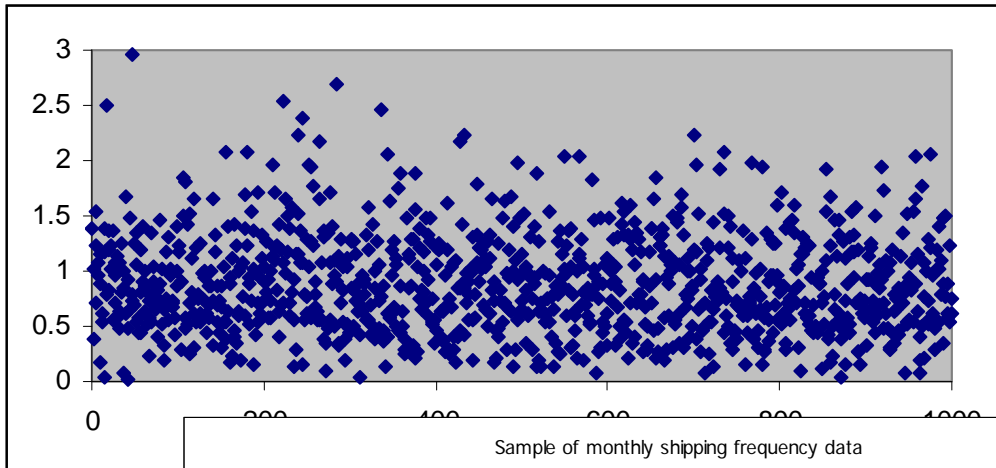
- Expert opinion
  - Survey
  - Individual interaction
- Data
  - Dataset
  - Survey
  - Literature

# Potential Stochastic Inputs

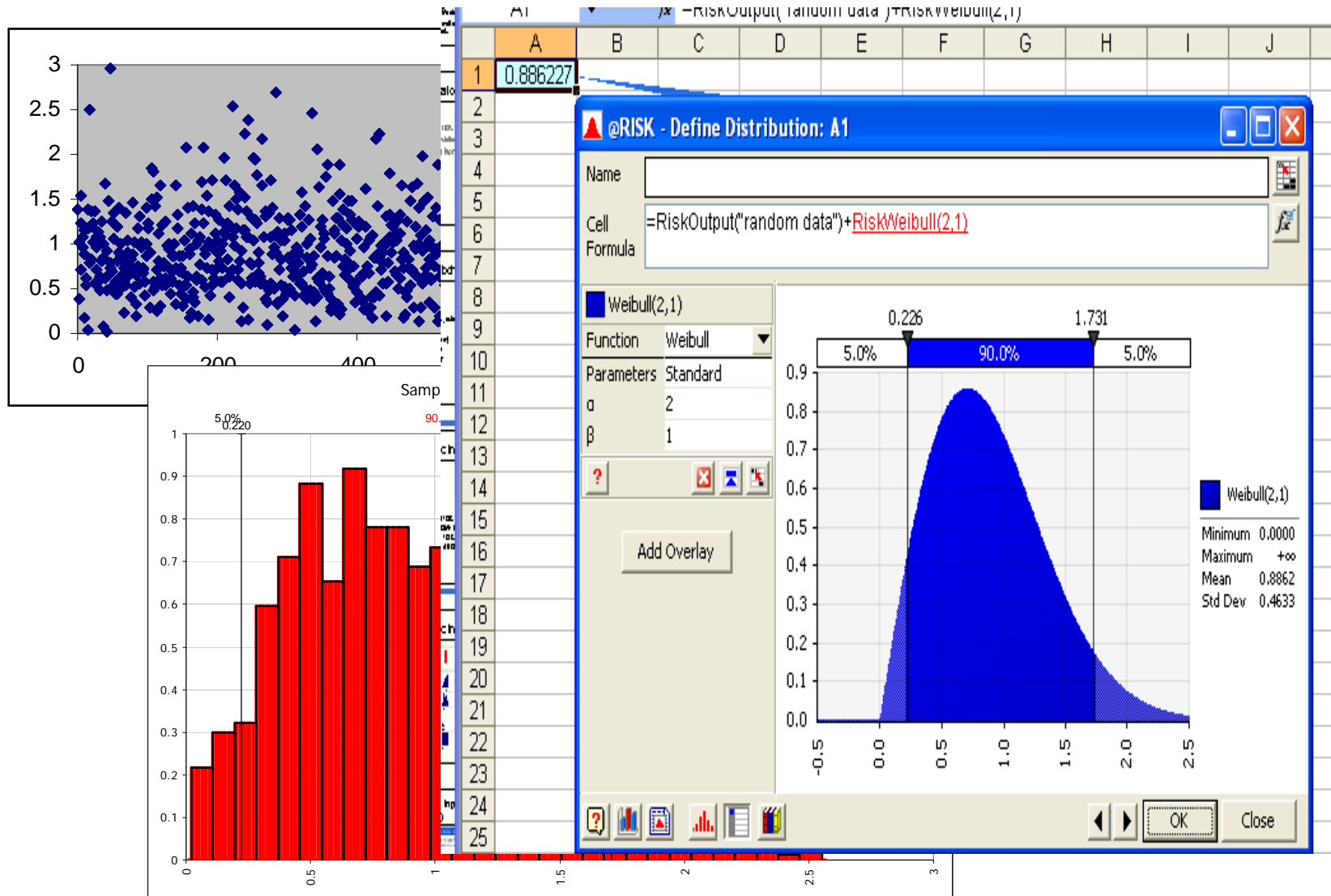


# Defining Stochastic Inputs

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# Defining Stochastic Inputs





# Stochastic modeling: Intraherd ex.

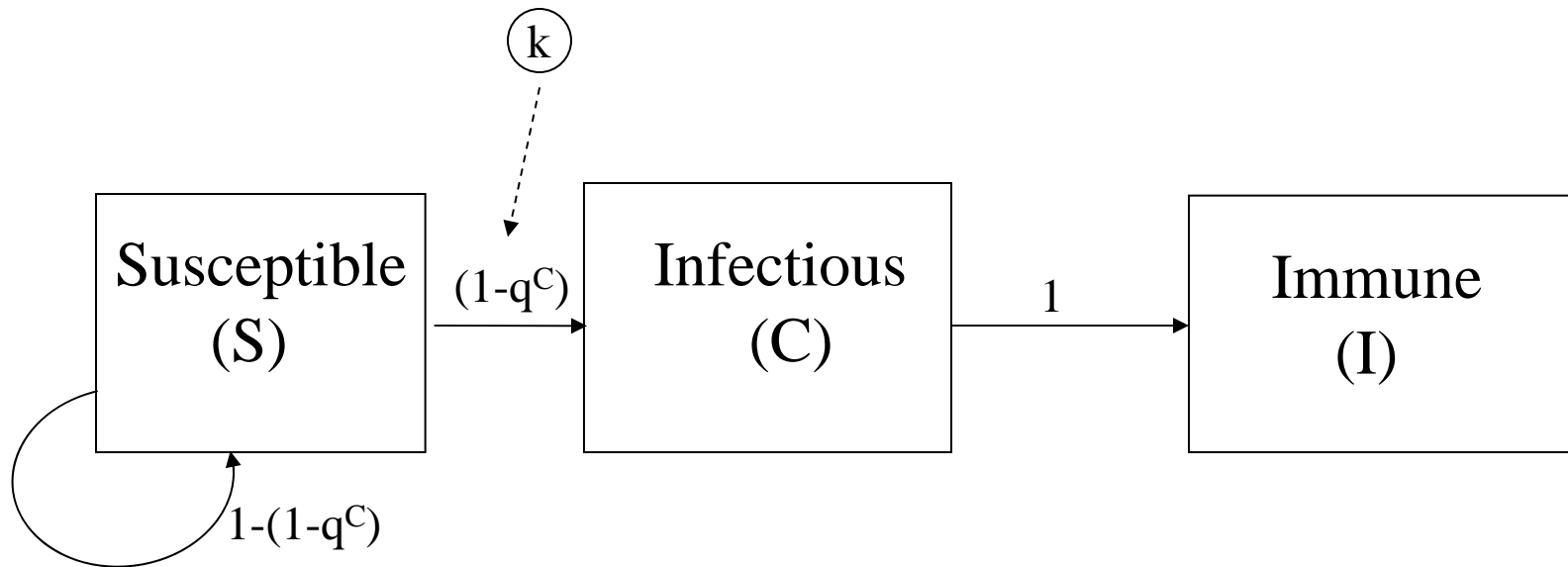
(number of adequate contacts ( $k$ ); health state durations ( $D_i$ ))

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- Deterministic
- Stochastic
  - Farm level
    - Dichotomous herd categorization
    - Homogeneous animal characteristics
  - Truly individual animal

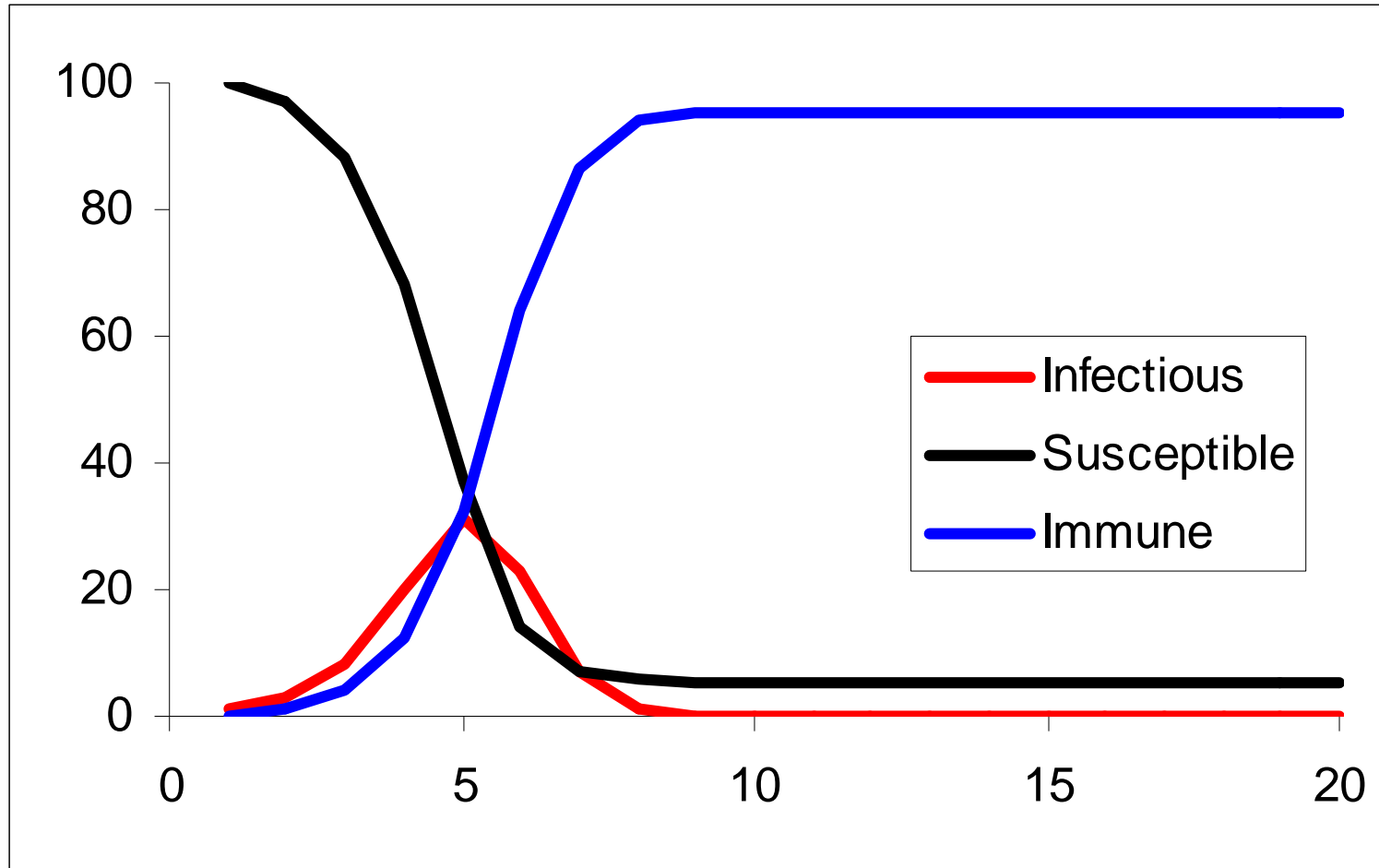


# Flow diagram of Reed-Frost (SIR) model



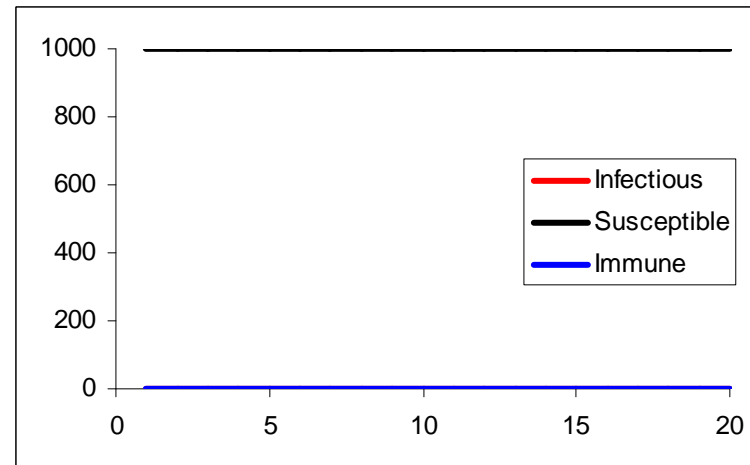
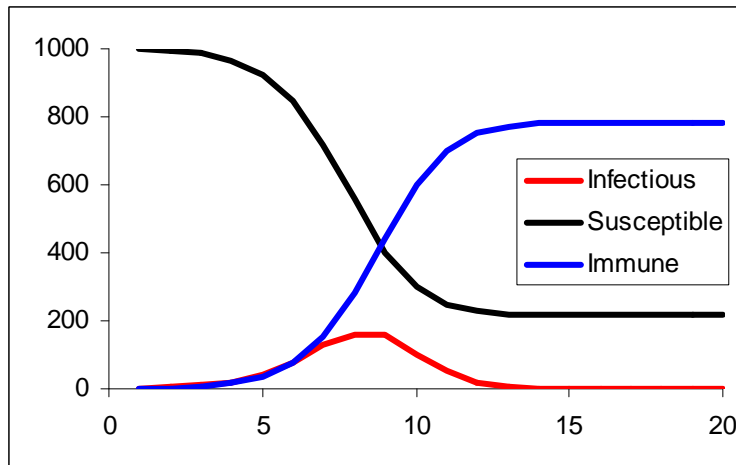
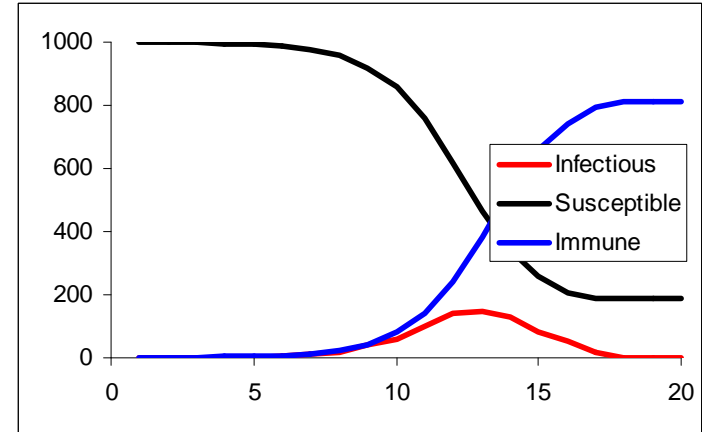
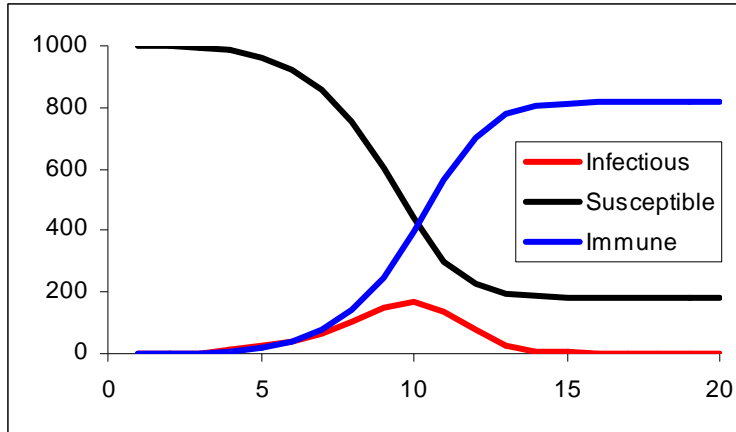


# Deterministic SIR Model



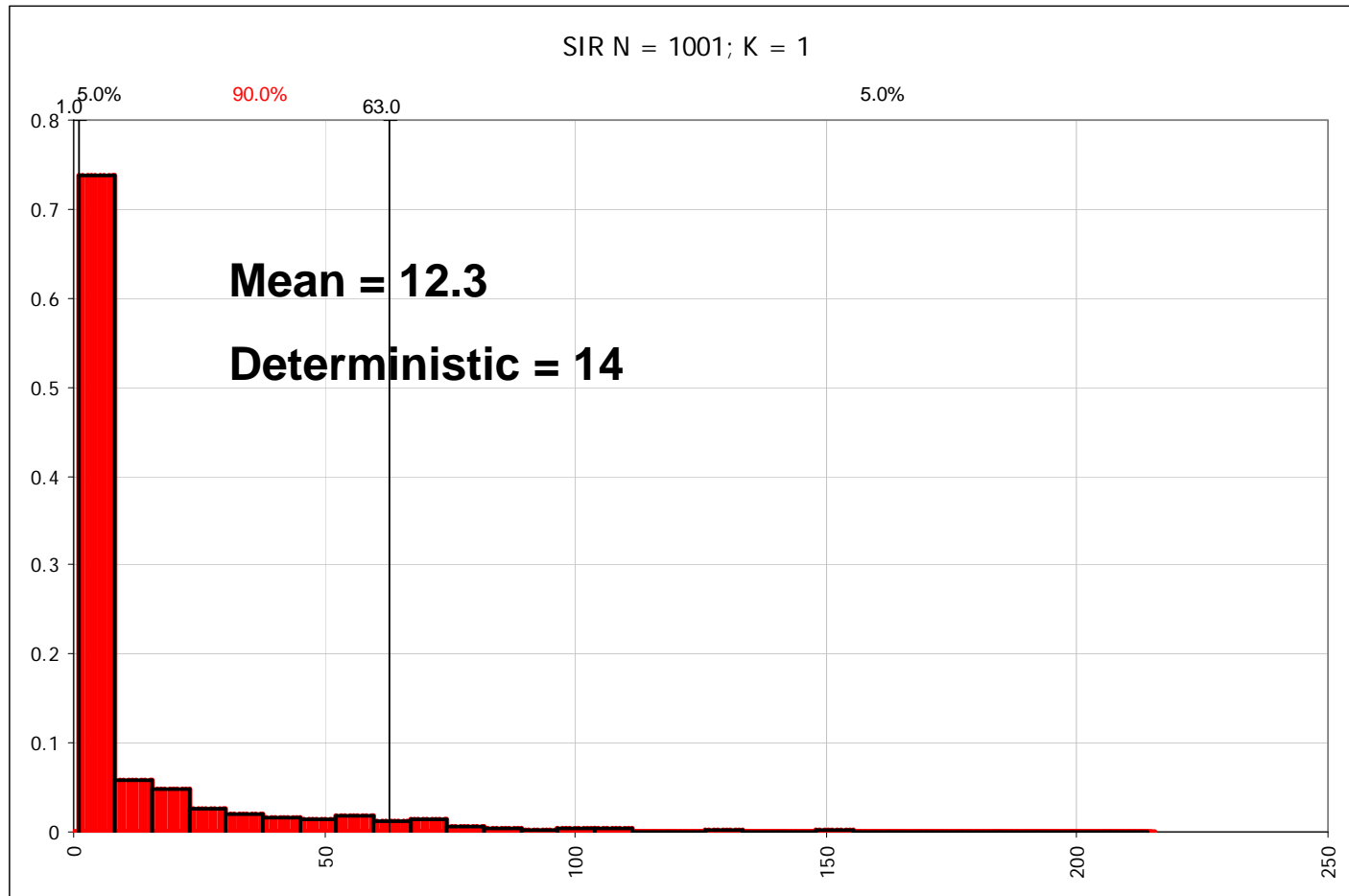
# Stochastic SIR Model

( $N = 1001$ ,  $K = 2$ )



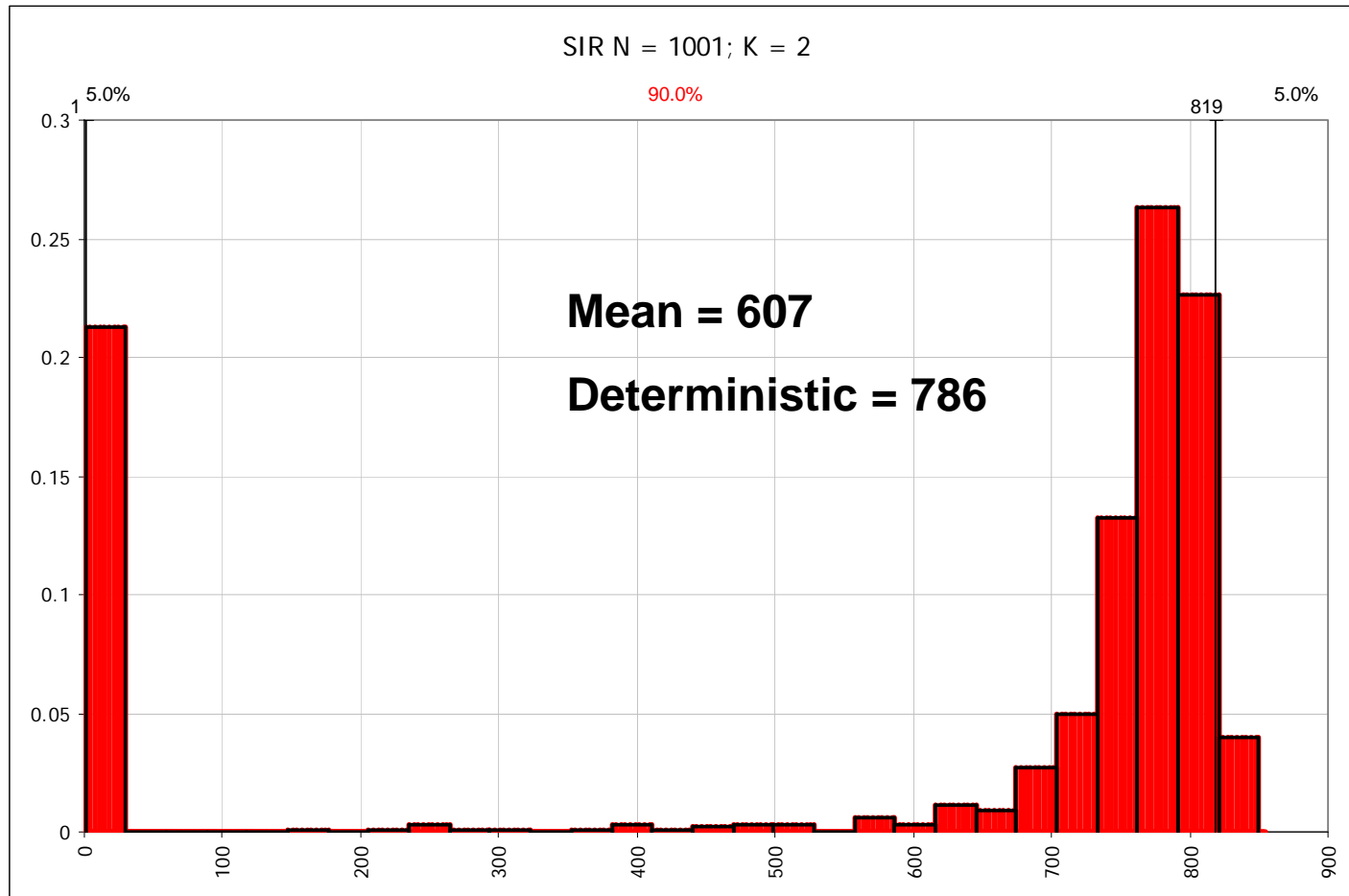


# Stochastic SIR Model



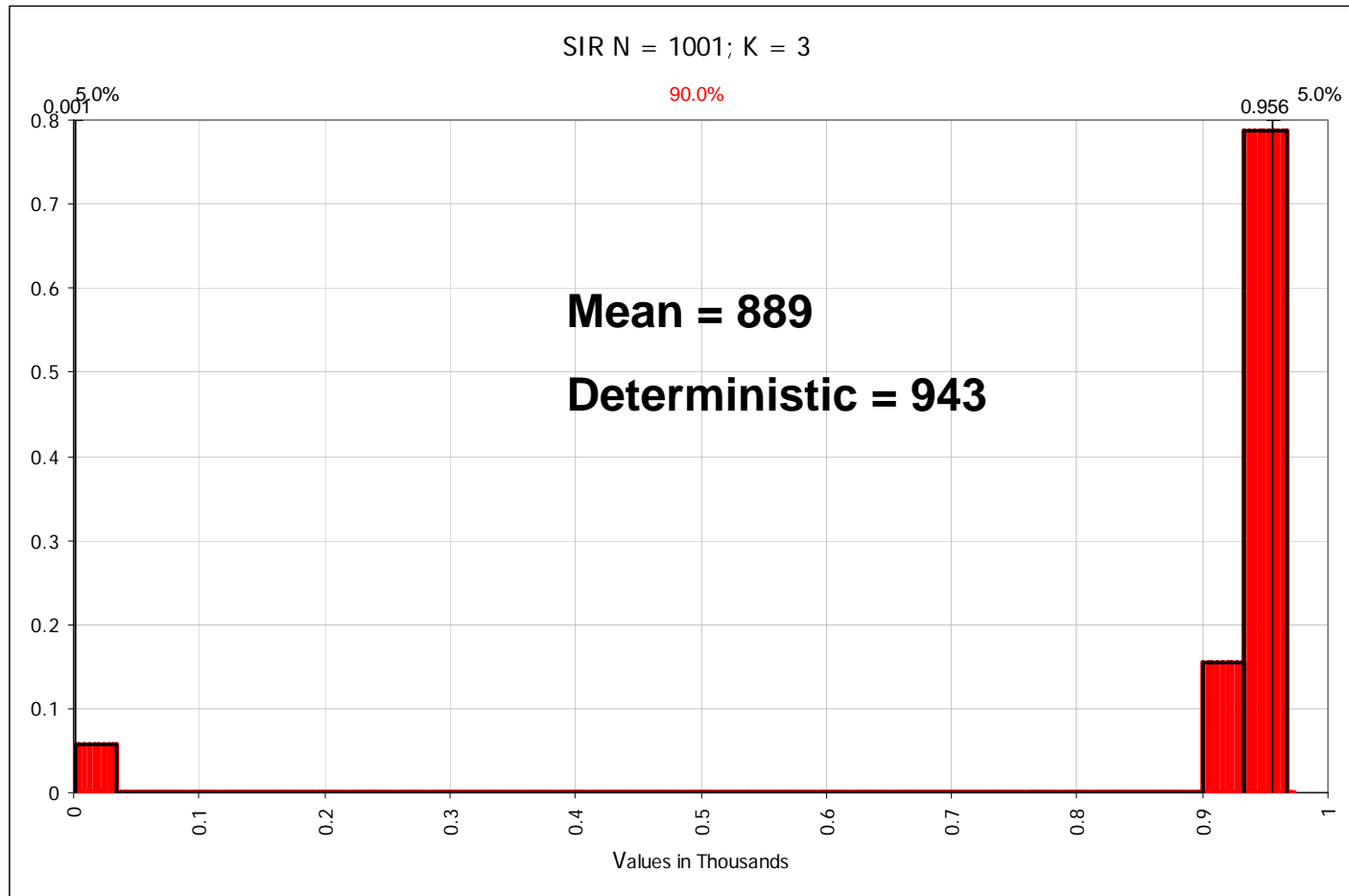


# Stochastic SIR Model



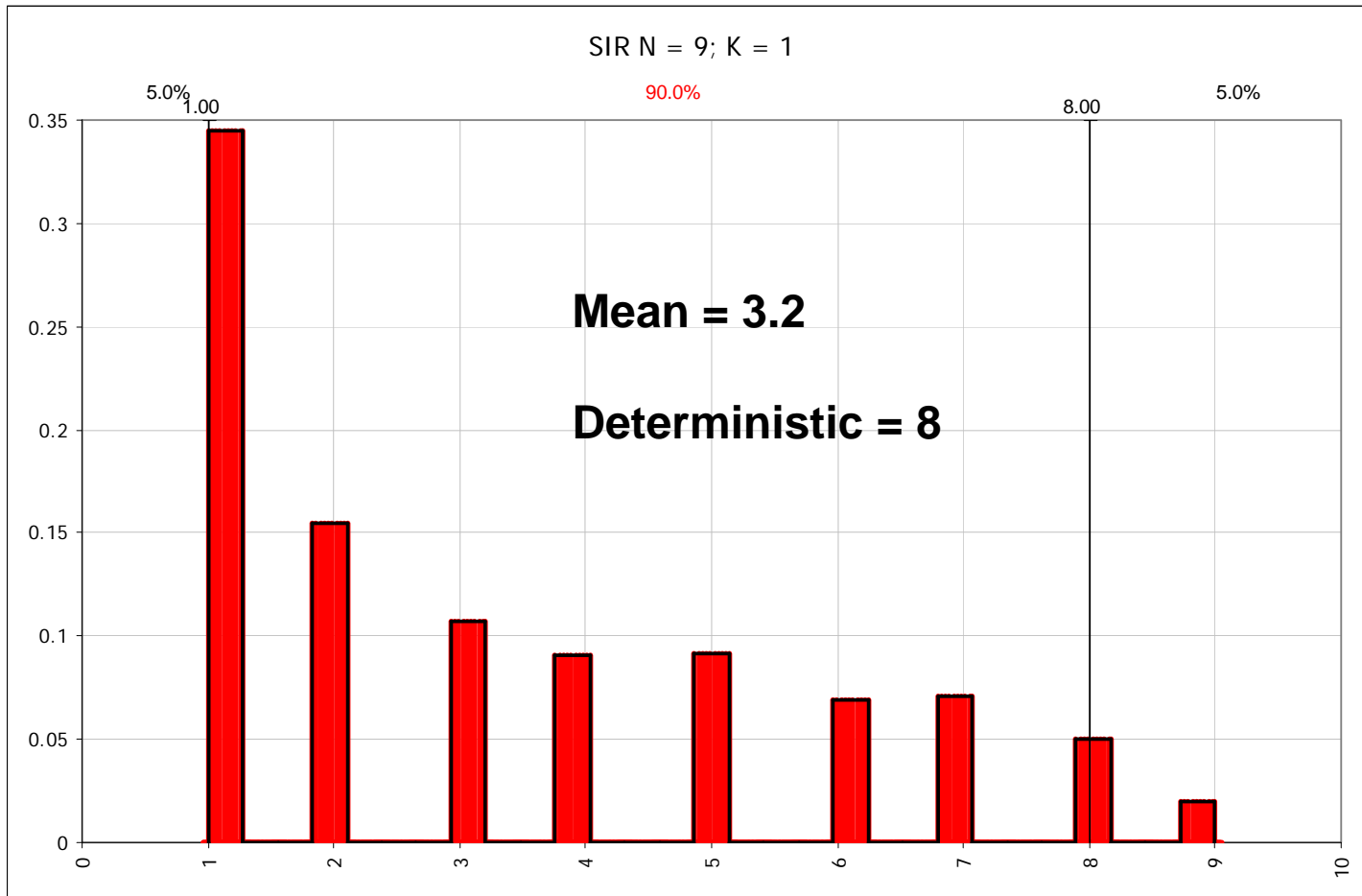


# Stochastic SIR Model



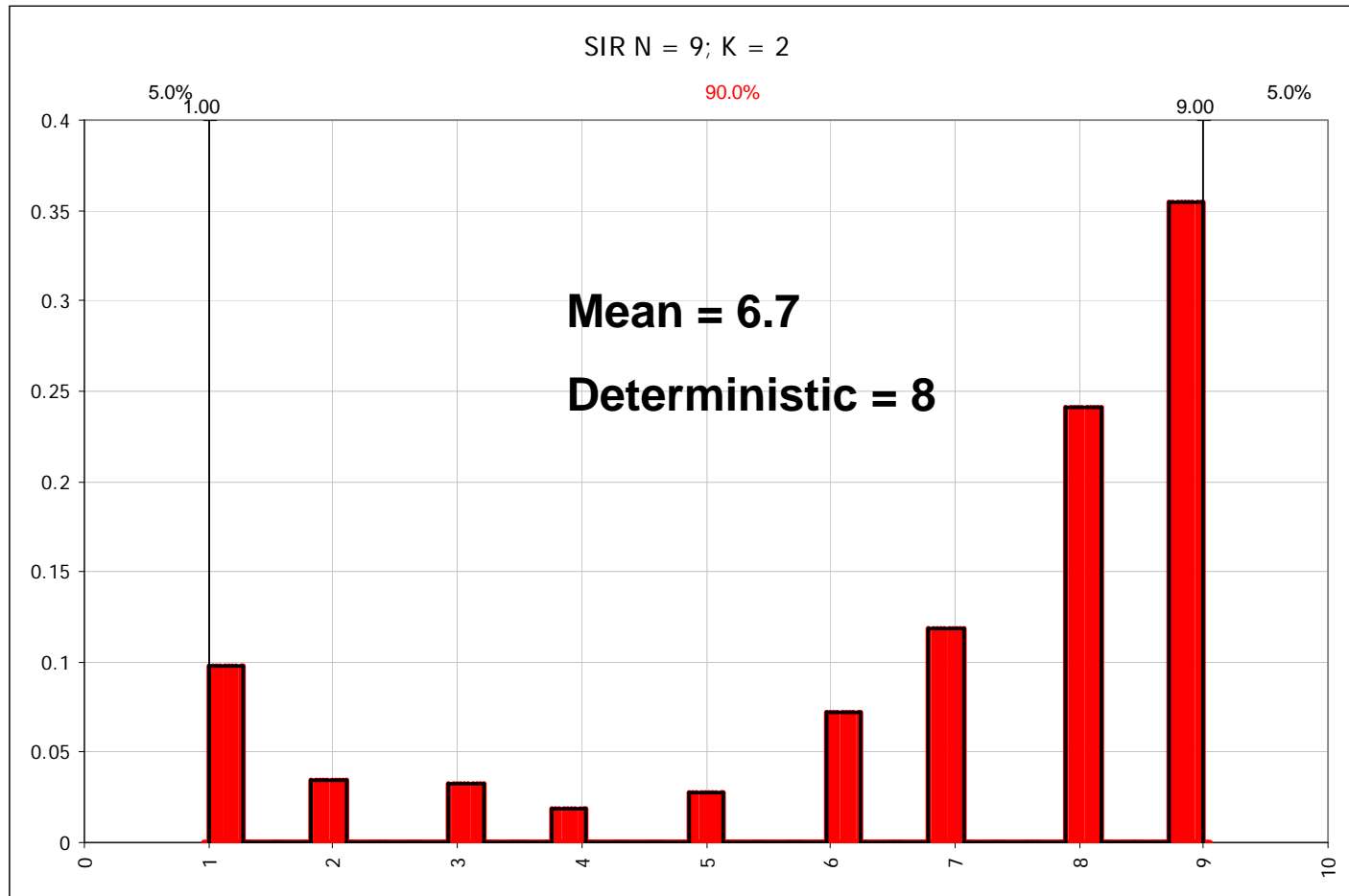


# Stochastic SIR Model





# Stochastic SIR Model

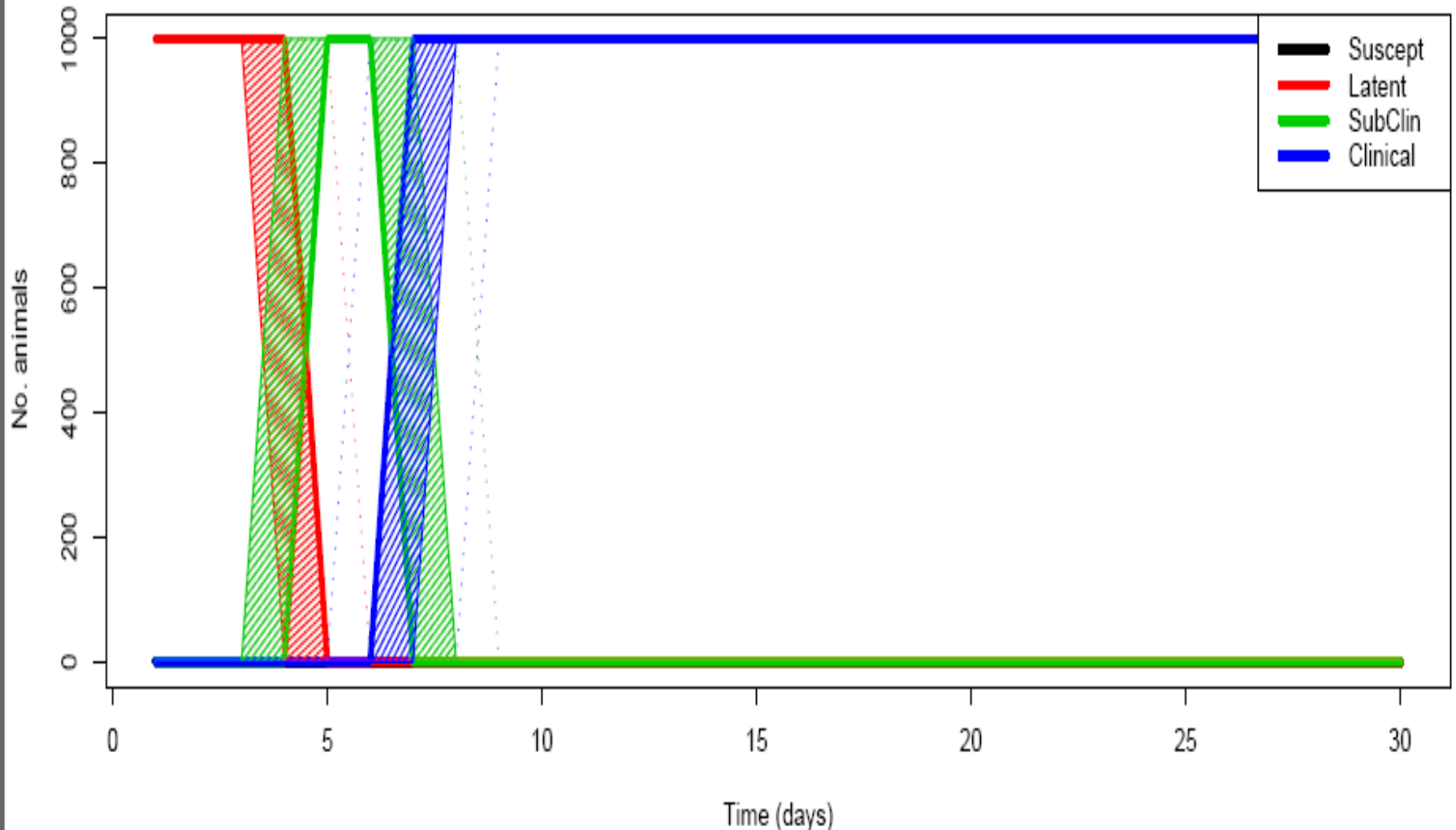






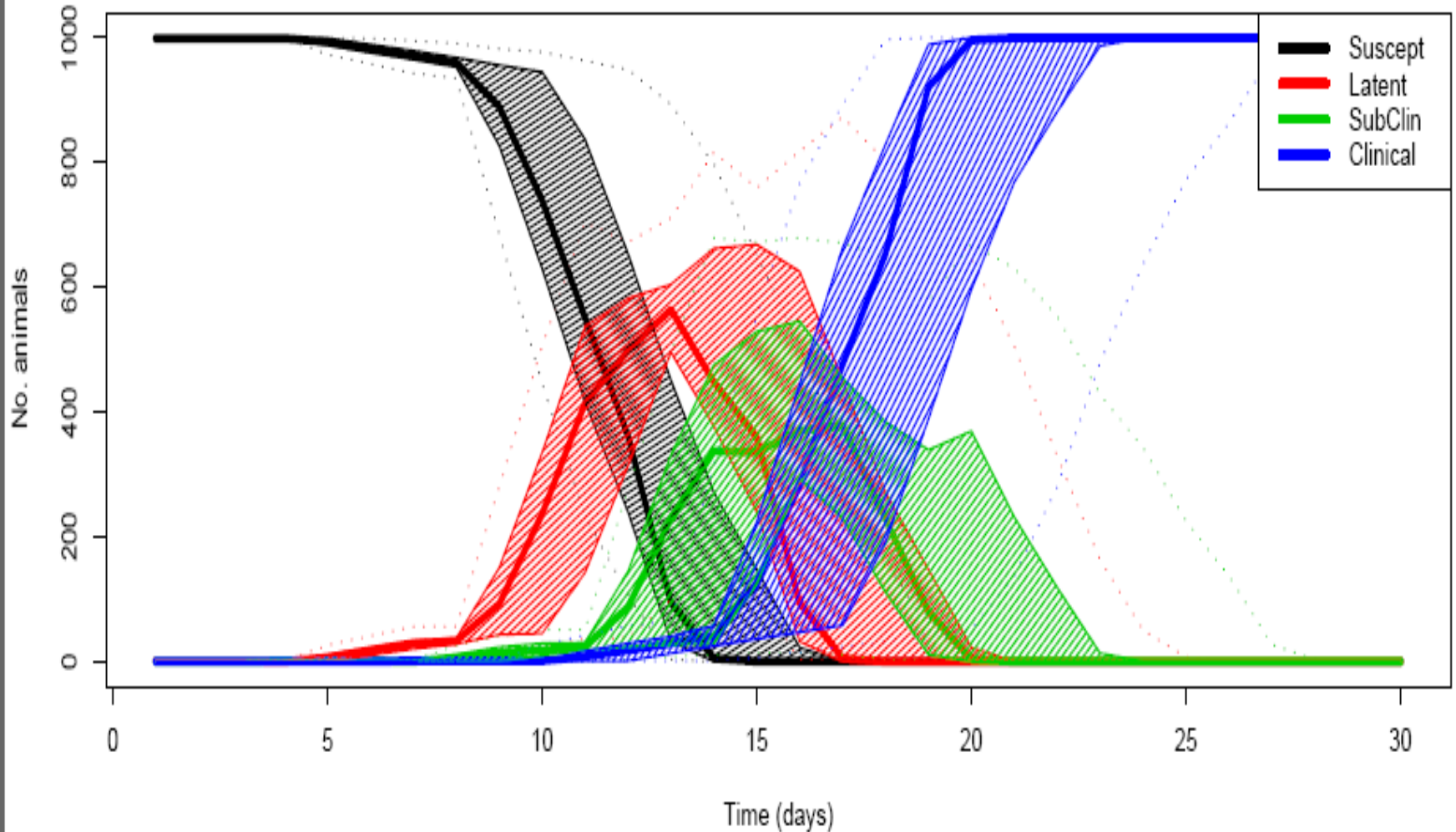
# Stochastic SLIC (no individual animal)

No individual animal model



# Stochastic SLIC (farm level)

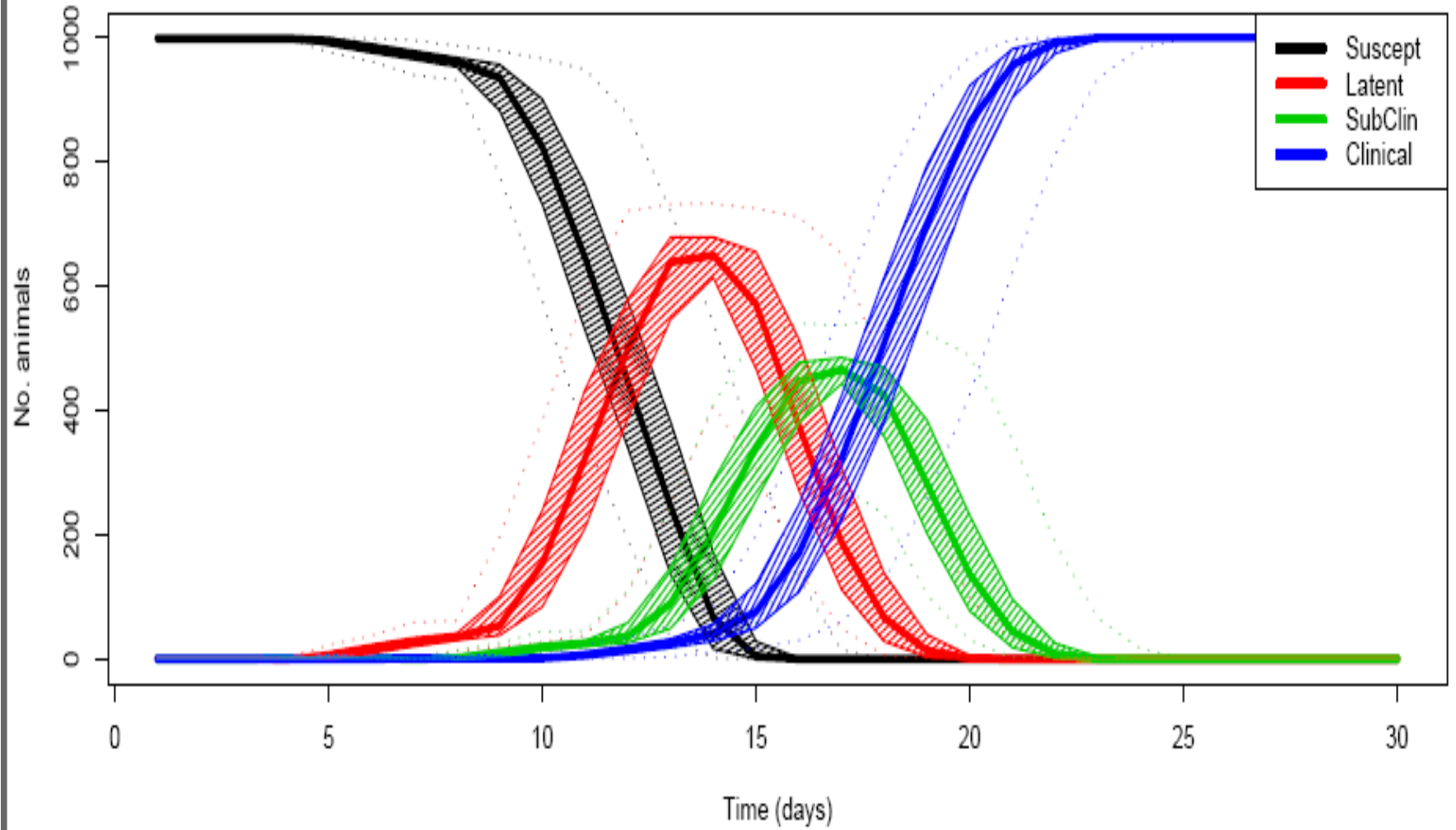
Durations distributed to farms





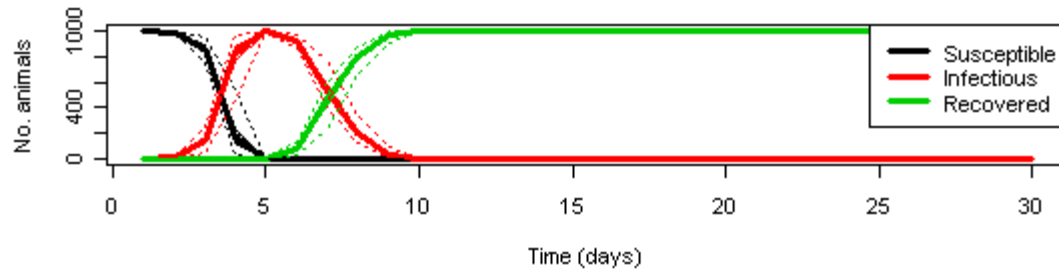
# Stochastic SLIC (true Individual Animal Based)

Durations distributed to individuals

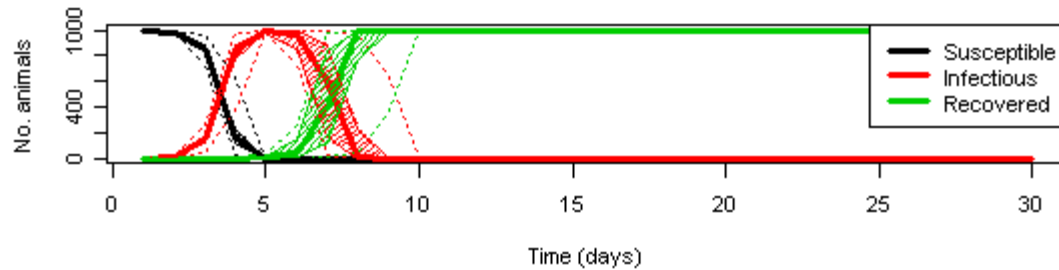


# SIR Models

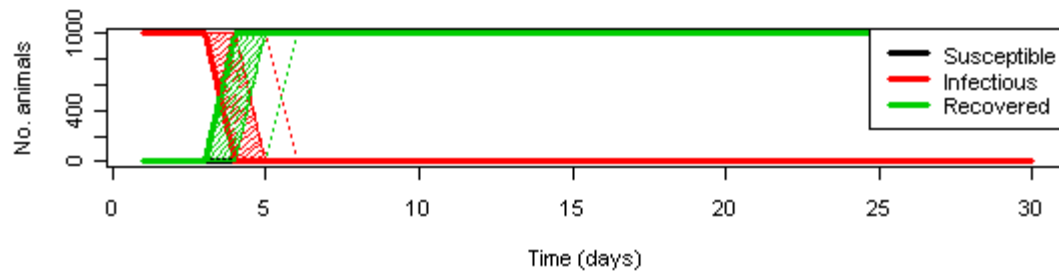
(SIR model)  
Durations distributed to individuals



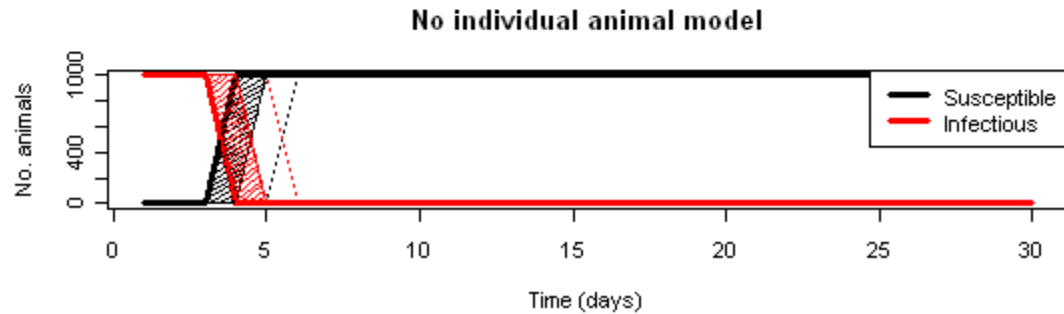
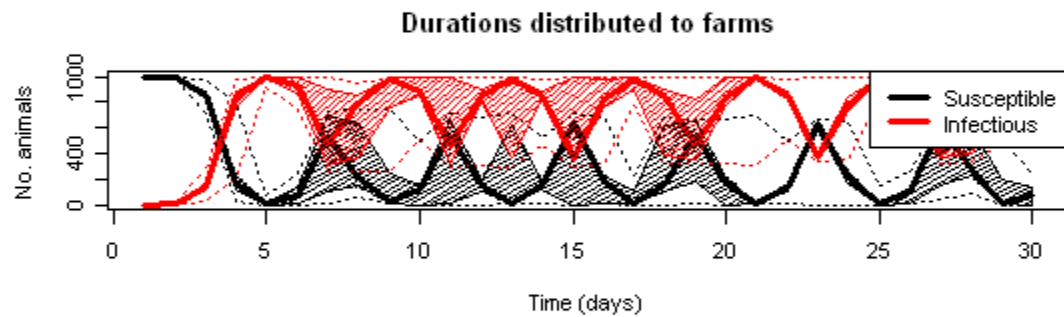
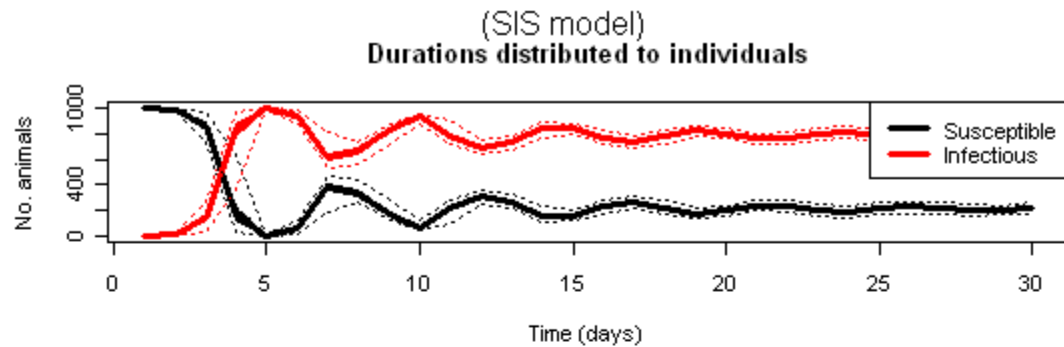
Durations distributed to farms



No individual animal model



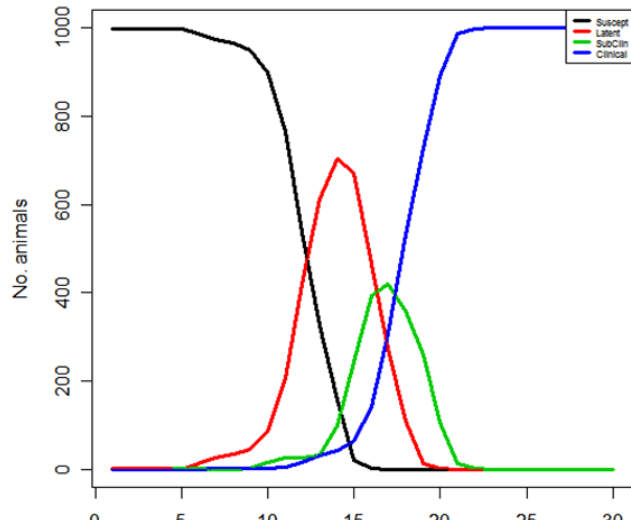
# SIS Models





# Deterministic vs. Stochastic IAB

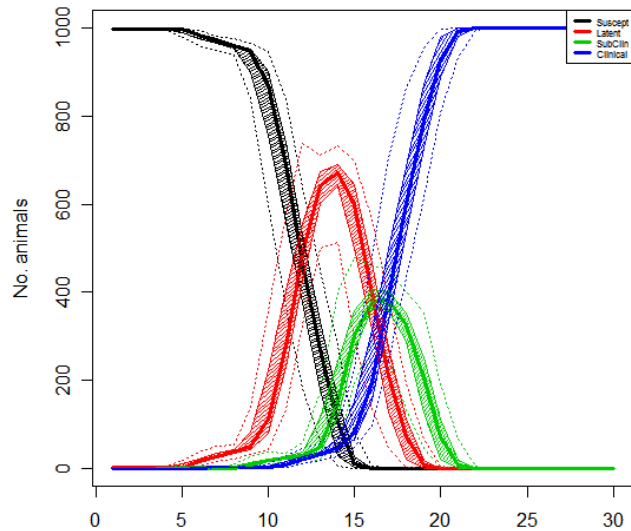
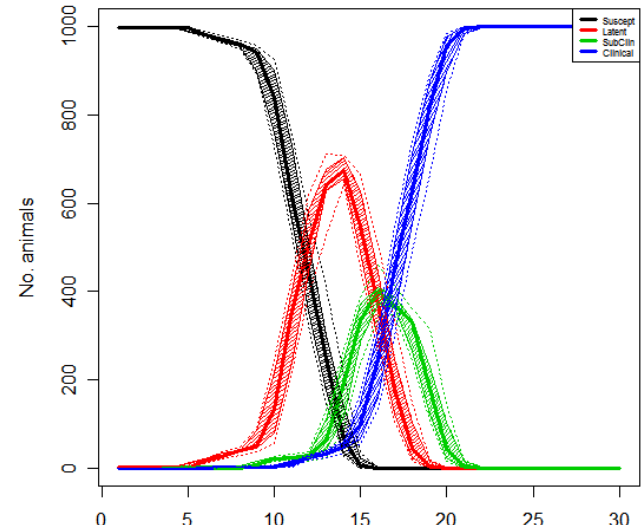
## SLIC Model (N = 1001; Iterations = 10, 100, 1000)



Iterations

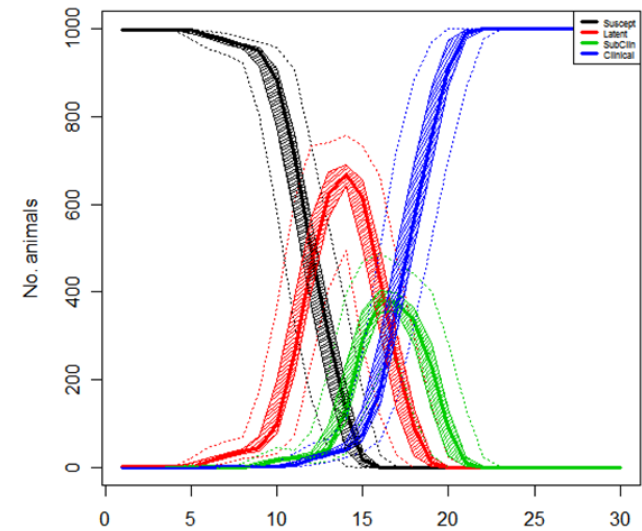
1

10



100

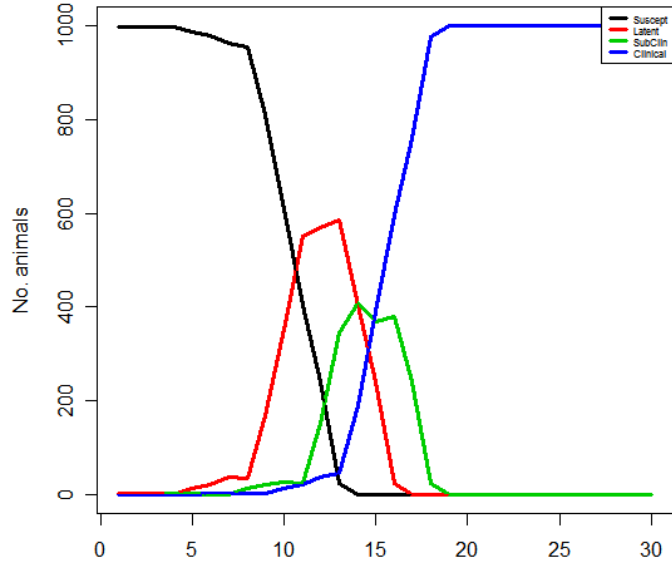
1000



Time (days)

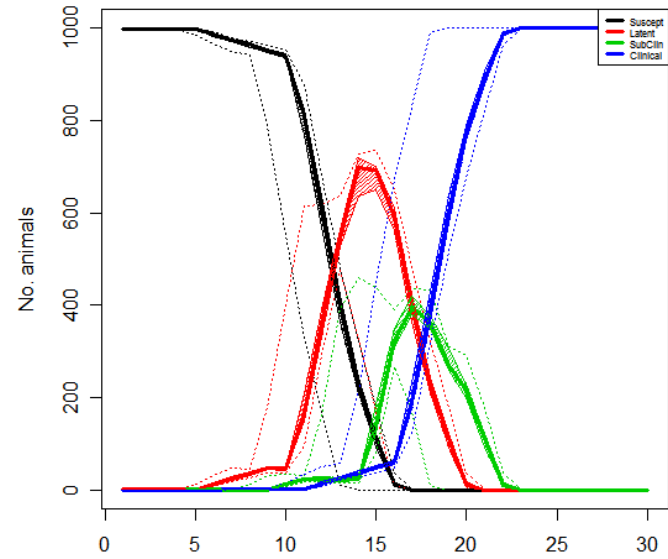
Time (days)

# Deterministic vs. Stochastic Herd Level SLIC Model (N = 1001; Iterations = 10, 100, 1000)

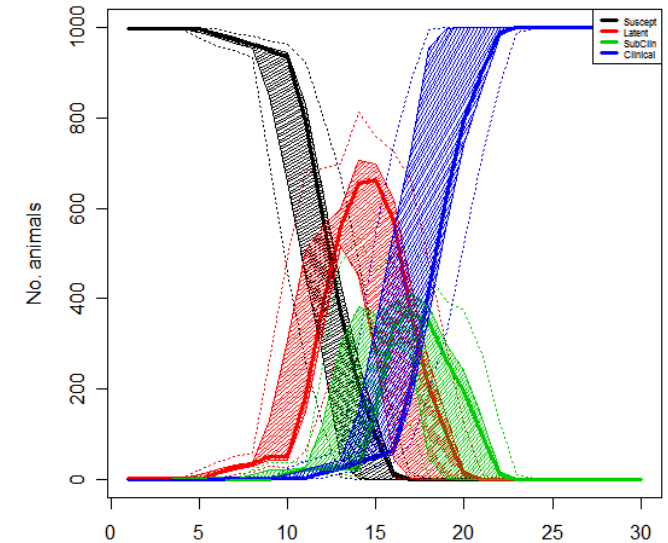
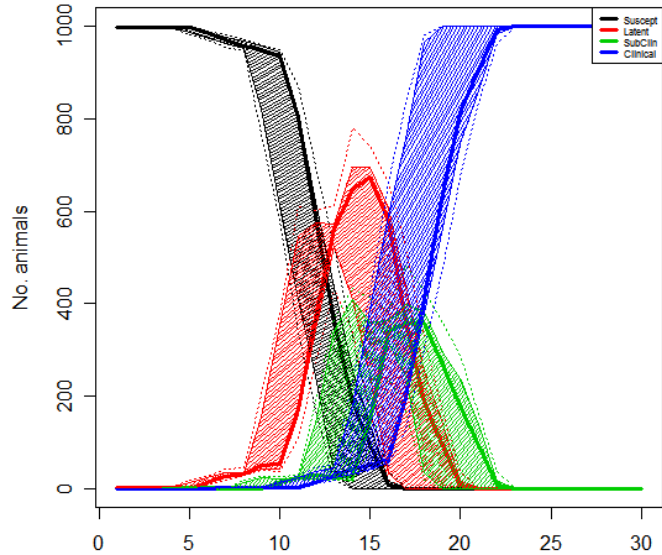


Iterations

1      10



100    1000



Time (days)

Time (days)



# Stochastic Model Conclusions

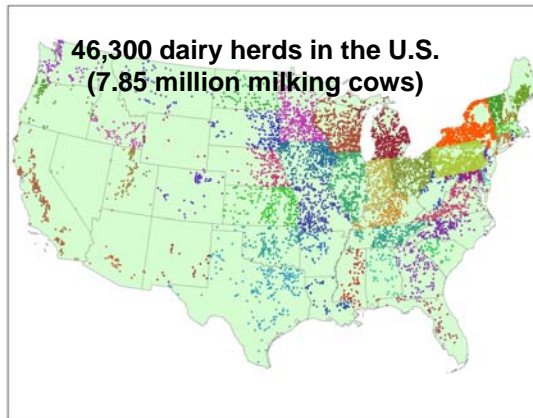
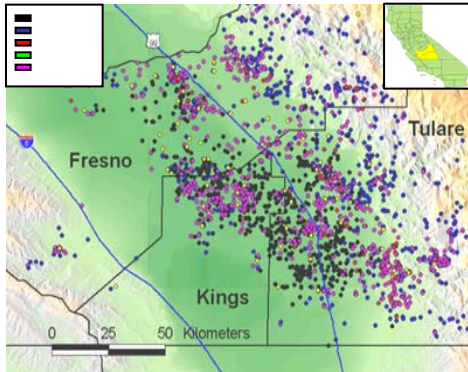
- Produce ranges of outcomes, which may provide more information than “average” results from deterministic models
- May avoid unreliable predictions resulting from epidemic “burn out”
- Caution should be used when using increased iterations (CIs vs. PIs)
- More (iterations) is better but “costs” more
- Require additional data/information



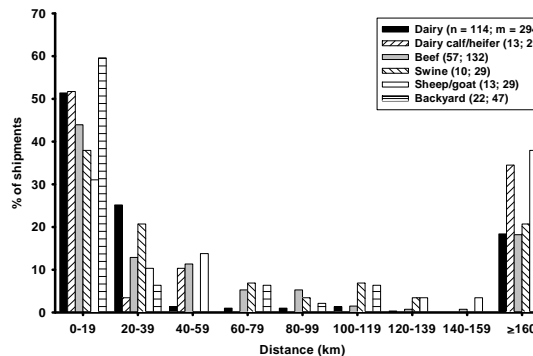
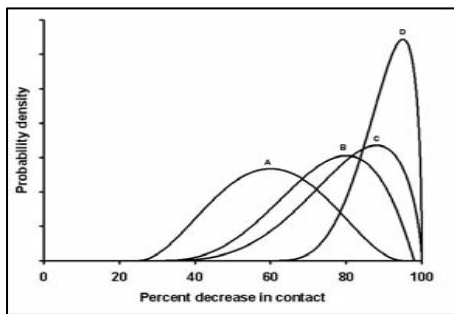
# Spatial Models

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# Davis Animal Disease Simulation (DADS) Model



- Spatial
- Stochastic
- Data driven
- Resource constrainable
- Highly individual animal based
- National level spread & control



- GENERAL LIVESTOCK -

Dr. Tim Carpenter, University of California - Davis, School of Veterinary Medicine, One Shields Avenue, Davis, CA 95616

## STUDY OF ANIMAL MOVEMENTS AND CONTACTS

Responses will remain strictly confidential.

1. Do you currently own or raise cloven-footed livestock?  Yes  No (Please return the questionnaire in the envelope provided and thank you for your time and interest)

2. How would you classify your herd or flock? (Circle all codes that apply)

CODE No.	HERD OR FLOCK TYPE	CODE No.	HERD OR FLOCK TYPE	CODE No.	HERD OR FLOCK TYPE
1	Beef (cow-calf)	8	Swine (farrow-to-wean)	15	Sheep (range/flock)

UC DAVIS  
VETERINARY  
MEDICINE



# Populating Spatial Models

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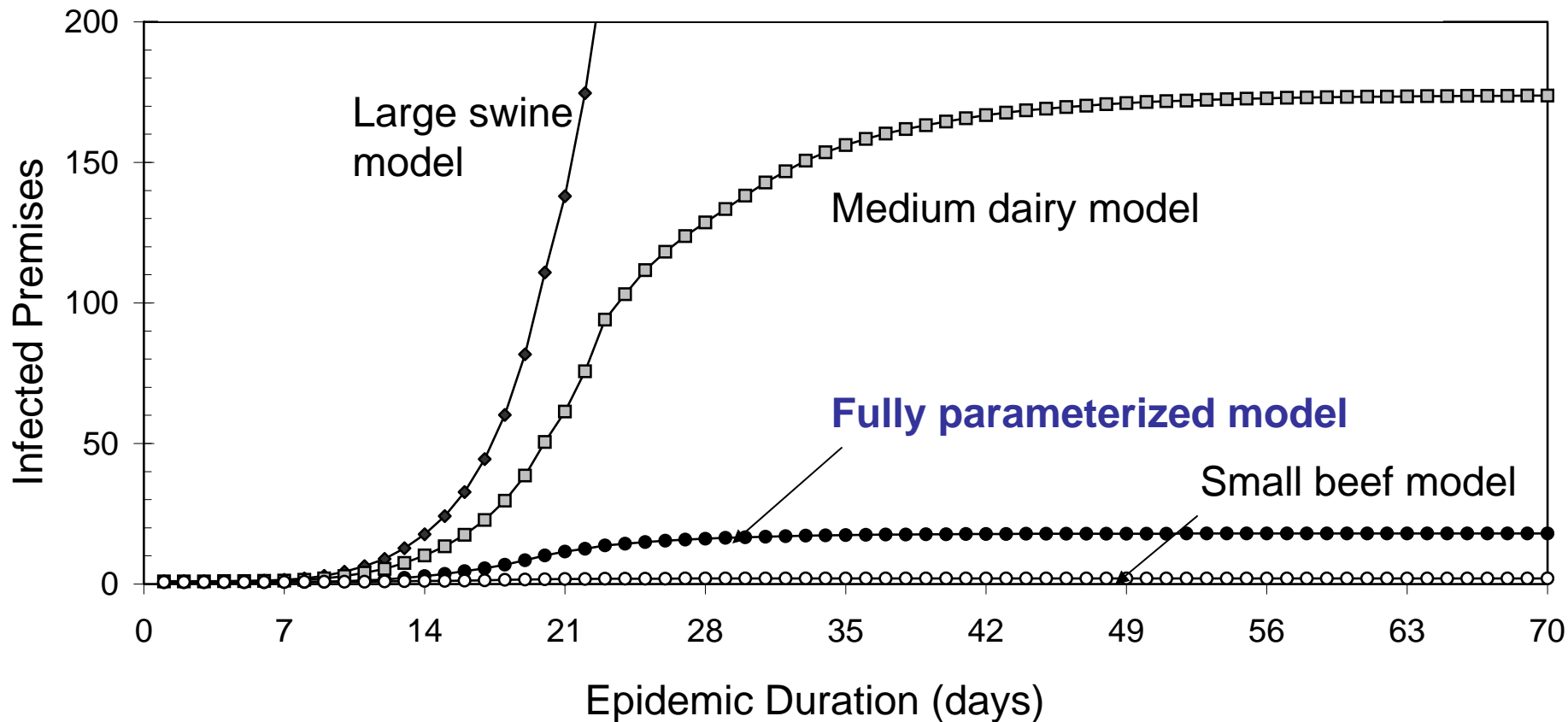
- Surveys
- Federal level data (USDA National Agriculture Statistics Service (NASS))
- Industry collaborators
- State collaborators
- Merged databases

# Use of heterogeneous operation-specific contact parameters changes predictions for foot-and-mouth disease outbreaks in complex simulation models

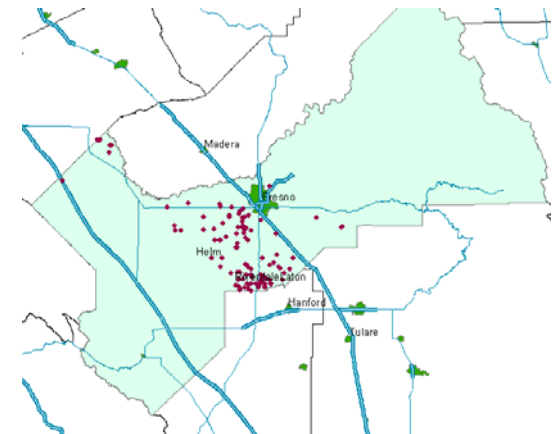
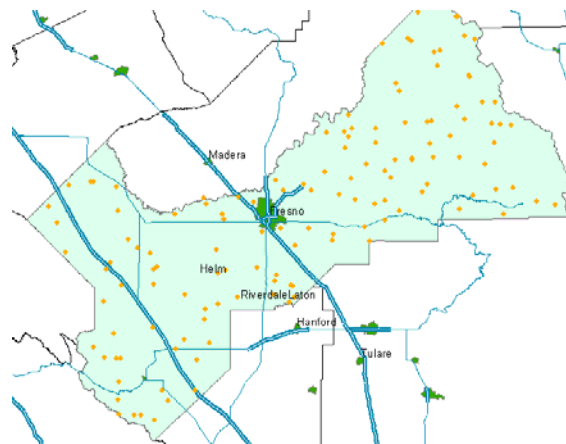
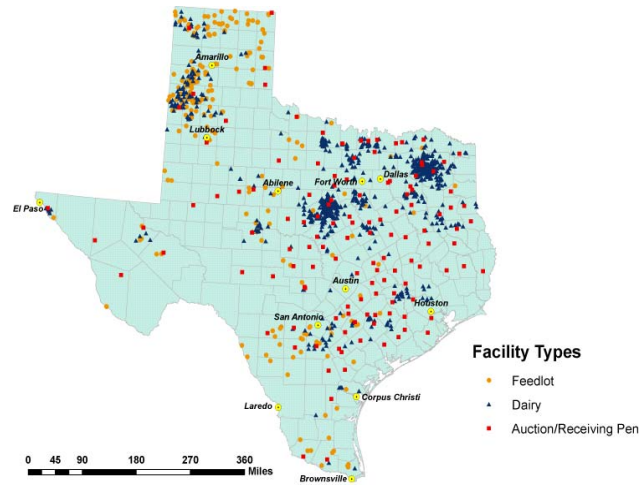
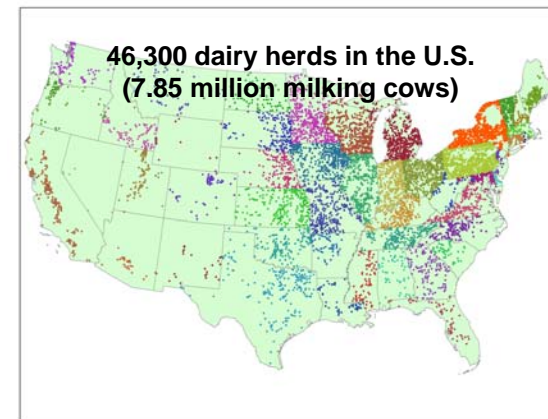
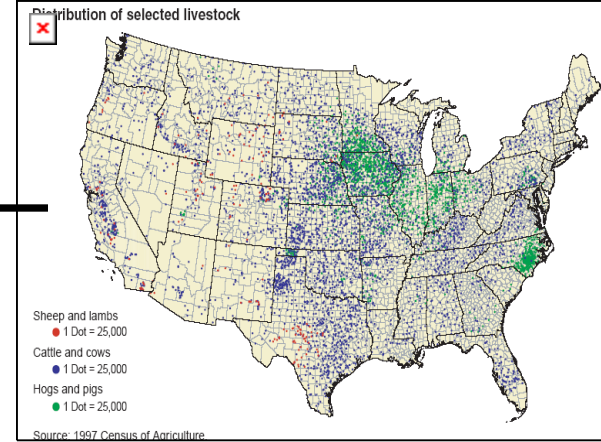
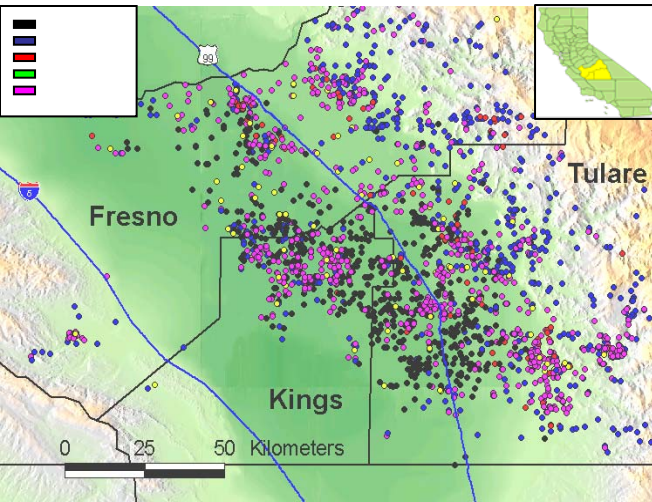
Bradley F. Dickey<sup>1</sup>, Tim E. Carpenter<sup>\*</sup>, Scott M. Bartell<sup>2</sup>

*Center for Animal Disease Modeling and Surveillance, VM: CADMS, Department of Medicine and Epidemiology, School of Veterinary Medicine, University of California, One Shields Avenue, Davis, CA 95616, United States*

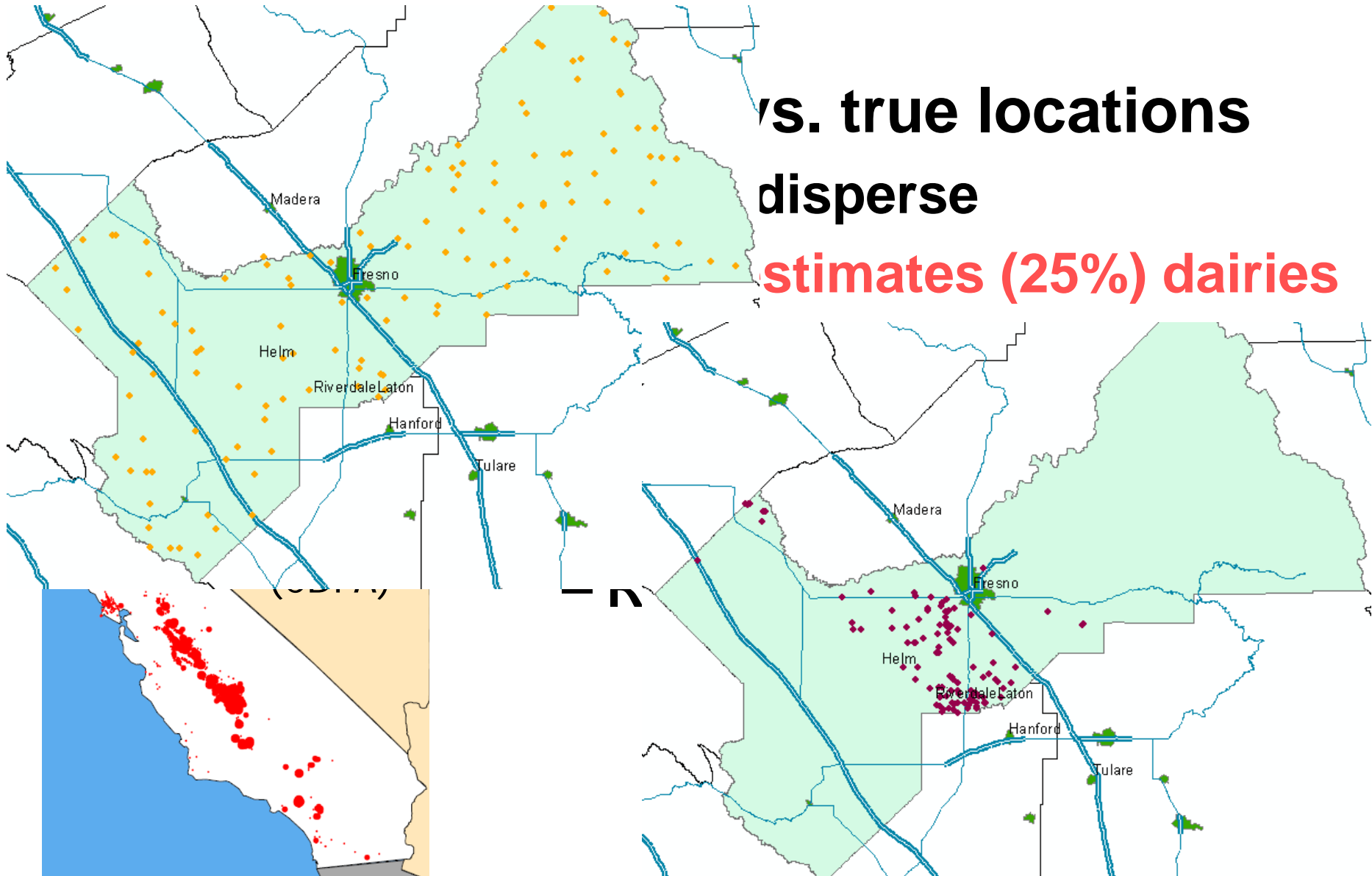
Received 21 November 2005; received in revised form 15 March 2008; accepted 24 April 2008



# Geographic Data

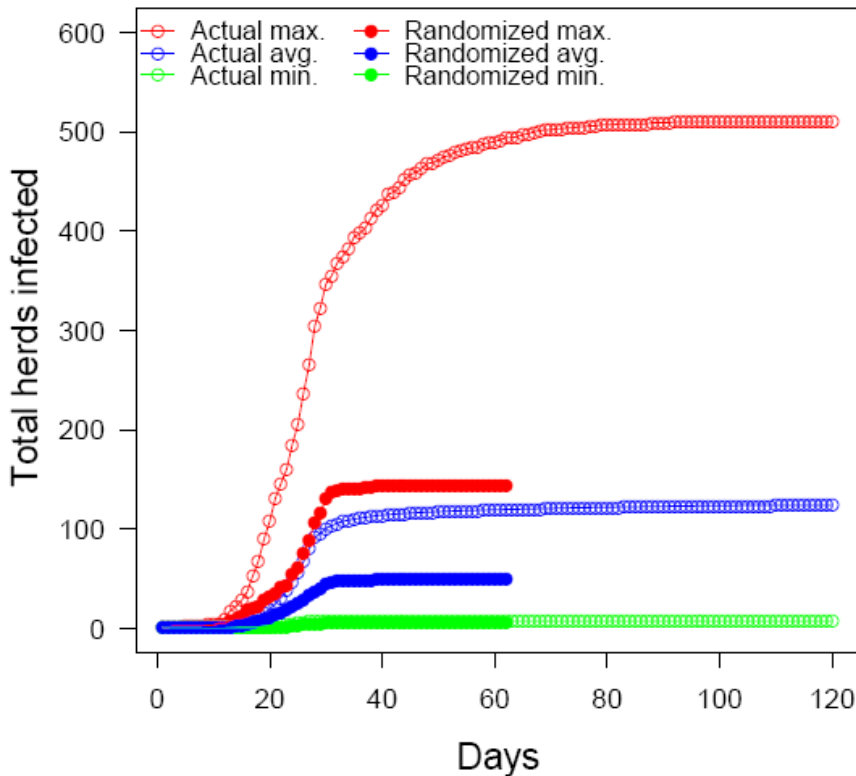


# Geolocation Data: CA Dairies



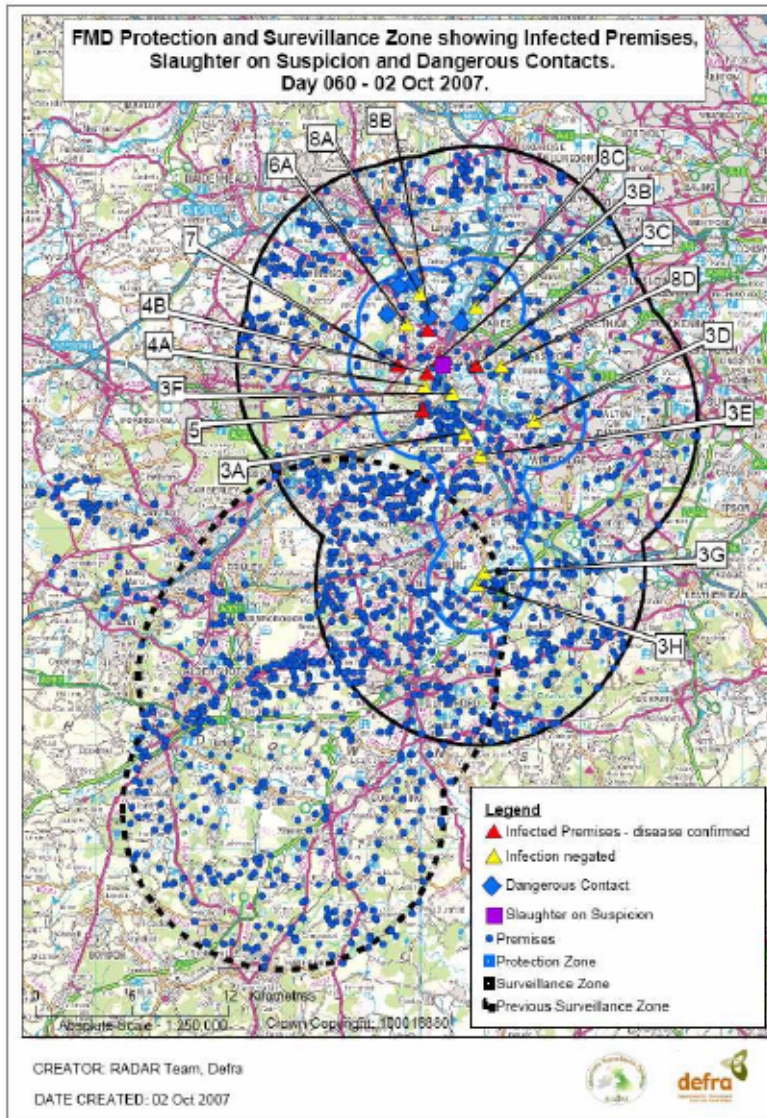
# Simulation Results: Random vs. Actual Locations

Predicted number of infected herds:  
actual vs. randomized dairy locations



- **NASS vs. true data sims.**
  - Min. similar but early end
  - Mean 60% underestimate
  - Max. 75% underestimate
- **Implications**
  - Underestimates epidemic impact and duration
  - Potentially misdirects resources
  - No info. > misinformation?

# Circular Controls in UK 2007

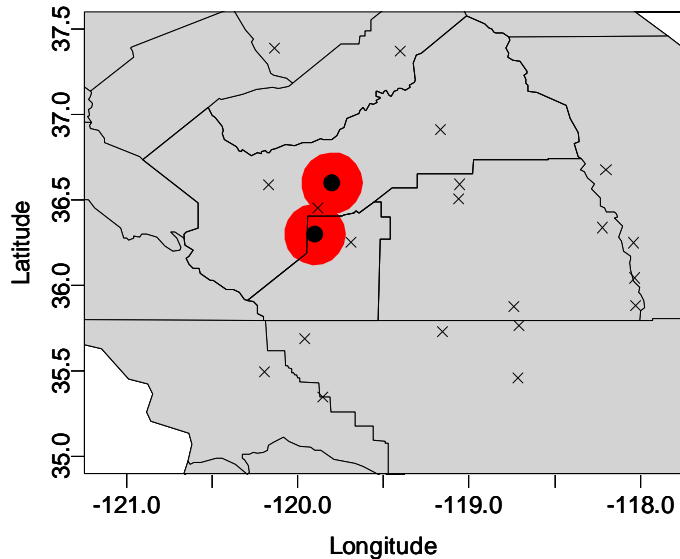


- Premises statuses updated daily
- “Target” constantly changing
- Resource allocation efficiency?
- Disease control impact?

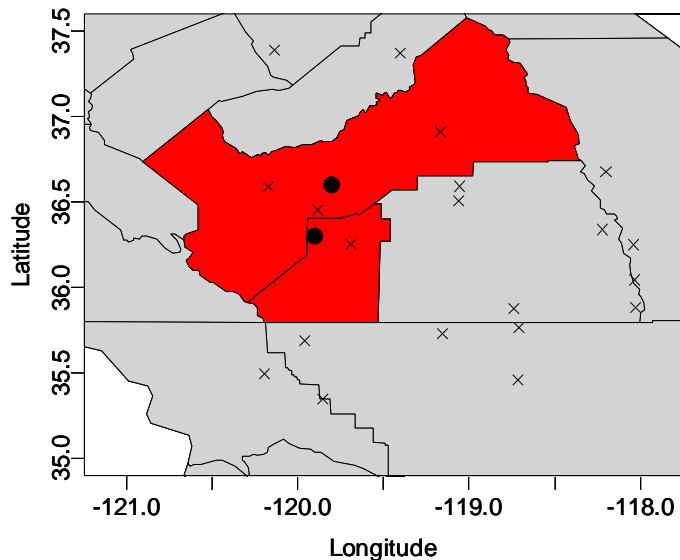


# Circular vs. Areal Surveillance

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- **Regional control benefits**
  - 10% decrease in IPs
  - 10% decrease in epidemic duration
  - 40% increase affected premises
  - 80% decrease in surveillance zone definition

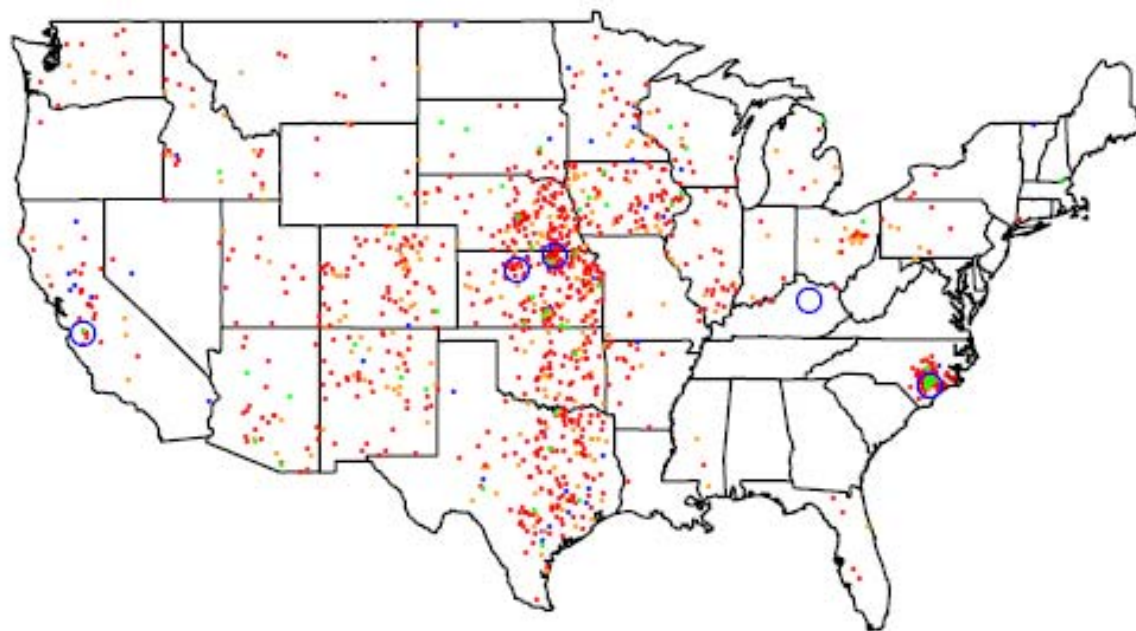


- **Additional applications**
  - Vaccination/culling
  - Movement
  - Expansion to states or regions vs. counties



Day: 20

- Latent
- Subclinical
- Clinical
- Immune
- Index herd



Intentional Introduction: 5 herds, 4 states



# Spatial Model Conclusions

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- Spatial models enhance visualization of an epidemic
- They may more accurately reflect spatial relationships, e.g. LAS, controls and spread
- Computationally, they make life very difficult



# Stochastic, Spatially Explicit Model Conclusions

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- Need for data
  - Spatial
  - Contact (DC, IDC)
- Need for complexity (stoch., spatial)
- Importance of model precision/predictability
- Need to consider model use during an epidemic with latent variable information



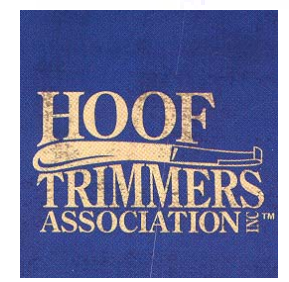
FARM BUREAU FEDERATION



Washington Cattlemen's Association



National Hog Farmer

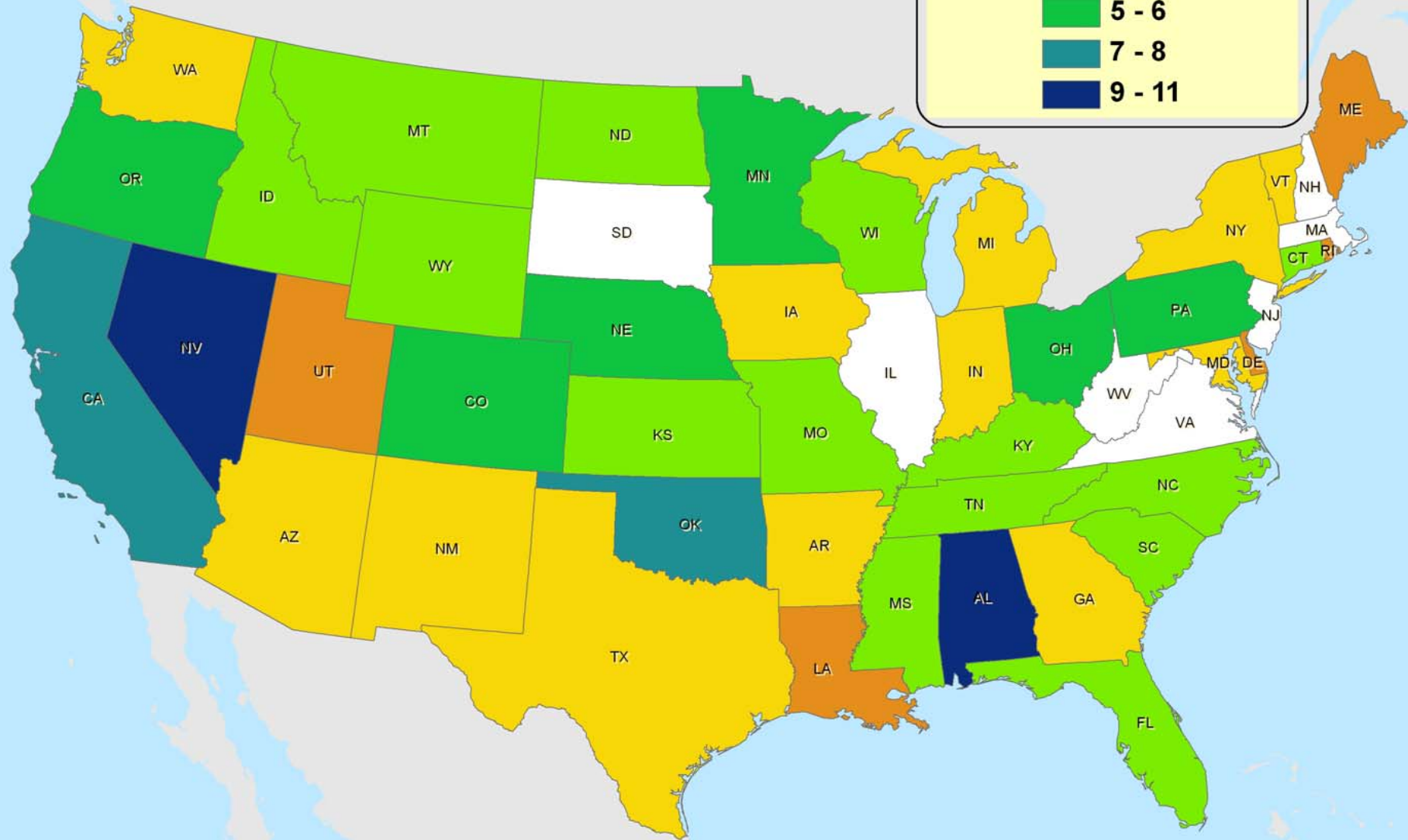


California Dairy Campaign



AK

### Number of Collaborations



# Funding

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FAZD CENTER



**Collaboration** – CADMS, CDFA, Texas A&M, WUD, CDC, PDHGA, CWGA, CCA, ARPAS, VMTRC, USDA, CDFG, ARE (UCD), LLNL, DK, UK, NZ





# Questions?

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